

# PP spherical-wave reflection coefficients for viscoelastic media

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# Reflection coefficients

**Use of the coefficients in:**

forward modelling (reflectivity, ray theory, etc.)

inverse modelling (AVO, AVA, etc.)

**Type of the coefficients:**

plane-wave reflection coefficients

spherical-wave reflection coefficients

# Reflection coefficients

## **PP plane-wave reflection coefficients:**

frequency independent

singularity at the critical point (infinite derivative)

maximum at the critical point (CP)

non-oscillating in sub- and over-critical region

problems with application in viscoelastic media

# Reflection coefficients

**PP spherical-wave reflection coefficients:**

frequency dependent

no singularity, smooth at the critical point

shift of the maximum behind the critical point

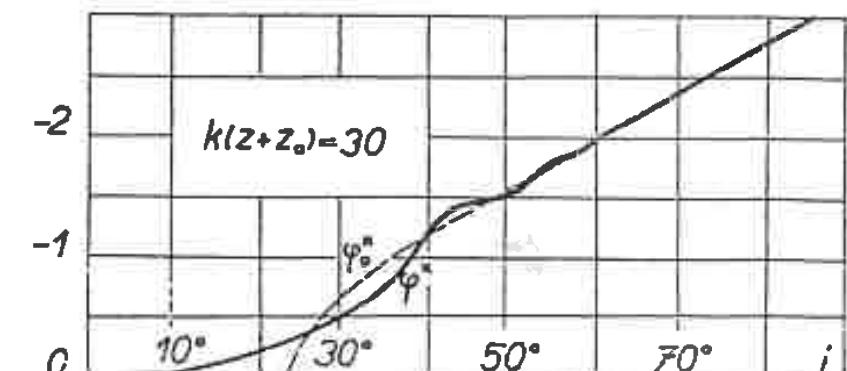
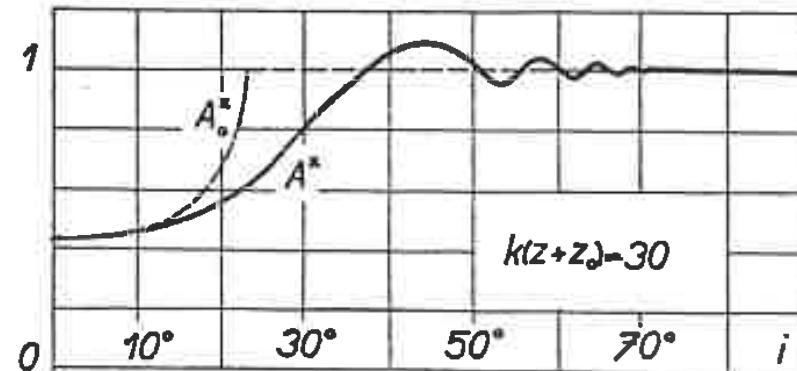
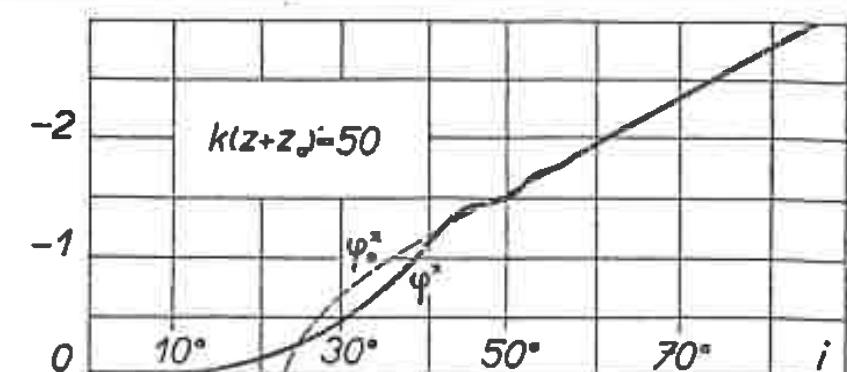
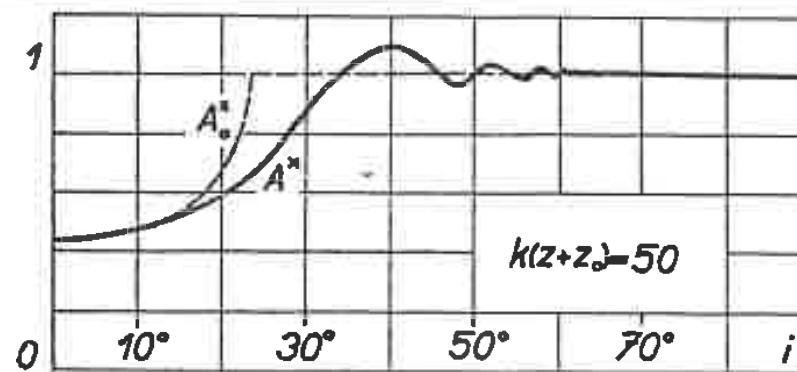
oscillations behind the maximum

rare application in viscoelastic media

⇒ **motivation to study the problem**

# Numerical examples

PP reflection due to a point source - HF asymptotic method  
(Červený and Hron, 1961. SGEG, 5, 122-132)

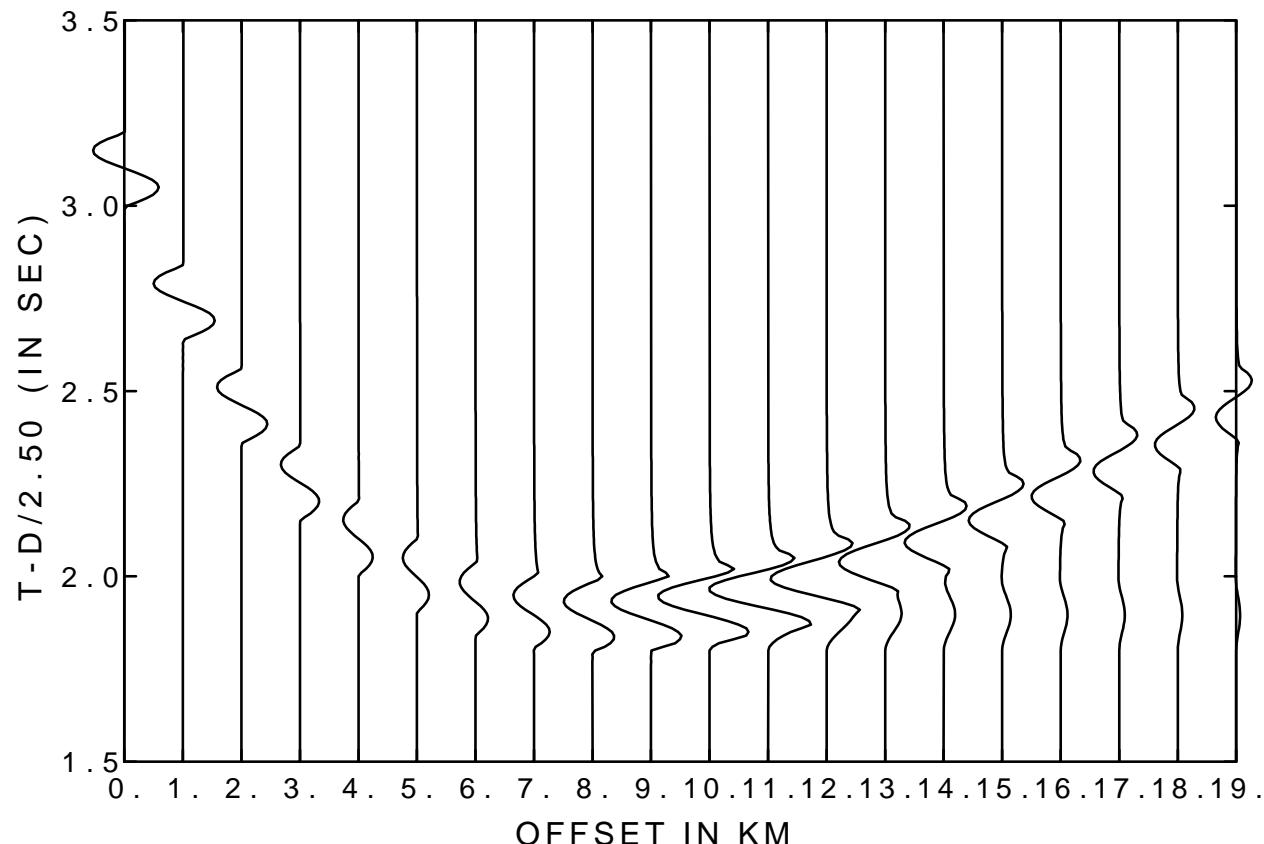


# Numerical examples

point-source PP reflection (CP - 8 km) - reflectivity (Wang, 1999)

$$\alpha_1 = 2.0 \text{ km/s}, \quad \beta_1 = 1.156 \text{ km/s}, \quad \rho_1 = 1.0 \text{ km/m}^3, \quad Q_1 = 10000$$

$$\alpha_2 = 2.5 \text{ km/s}, \quad \beta_2 = 1.445 \text{ km/s}, \quad \rho_2 = 1.1 \text{ km/m}^3, \quad Q_2 = 10000$$



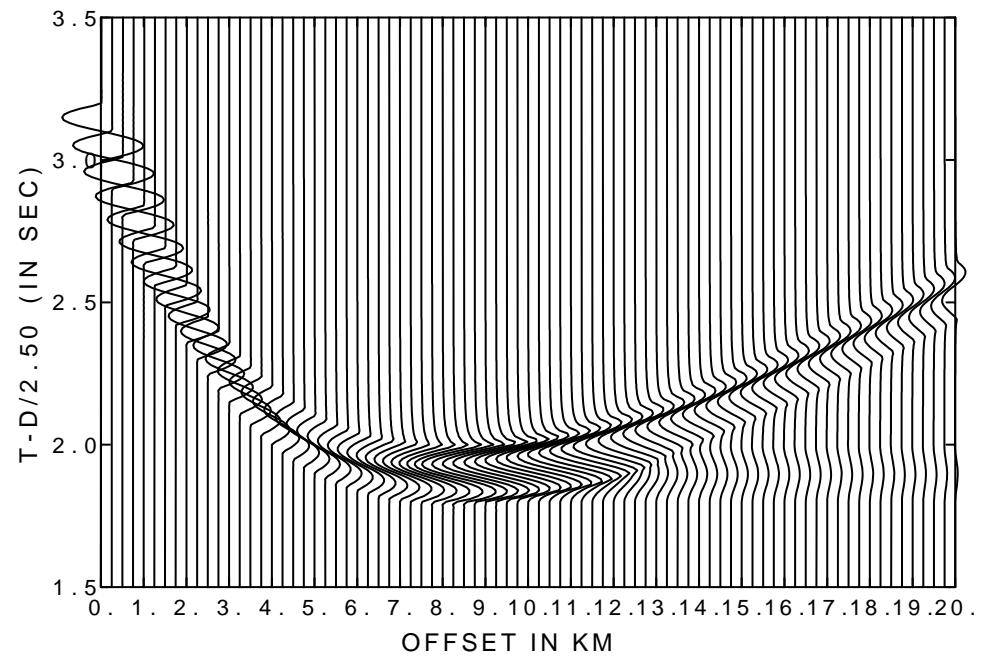
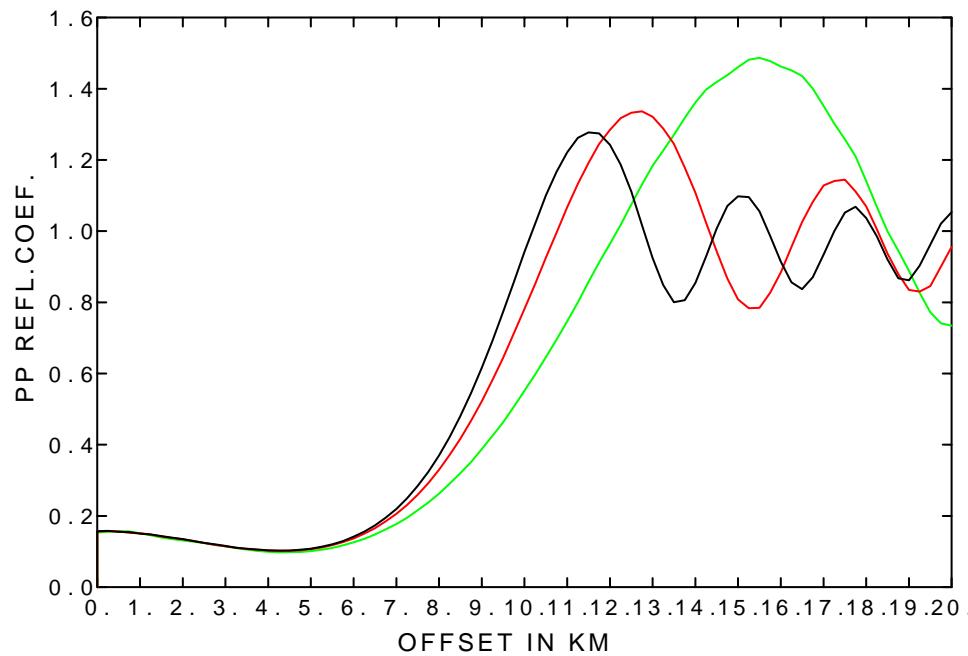
# Numerical examples

point-source PP seismograms and amplitudes (CP - 8 km) - reflectivity

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$$f = 10 \text{ Hz}, \quad f = 20 \text{ Hz}, \quad f = 30 \text{ Hz}$$



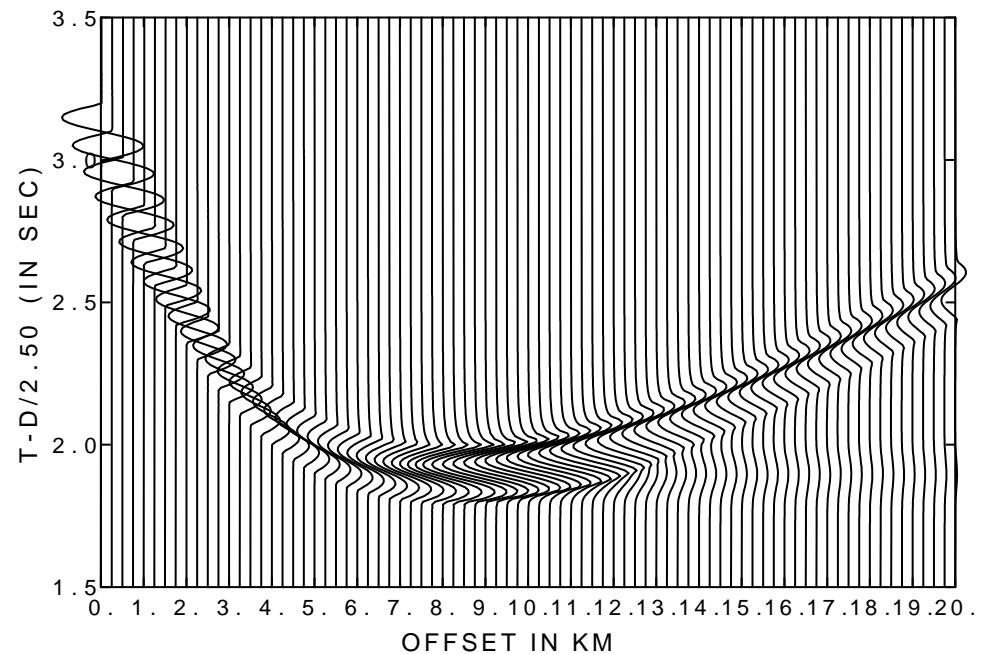
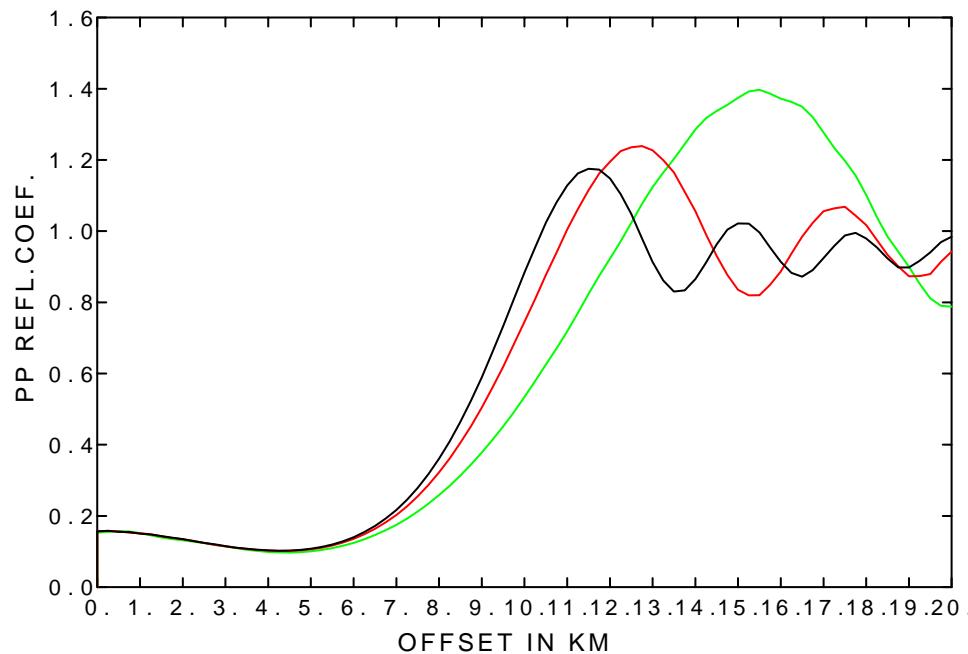
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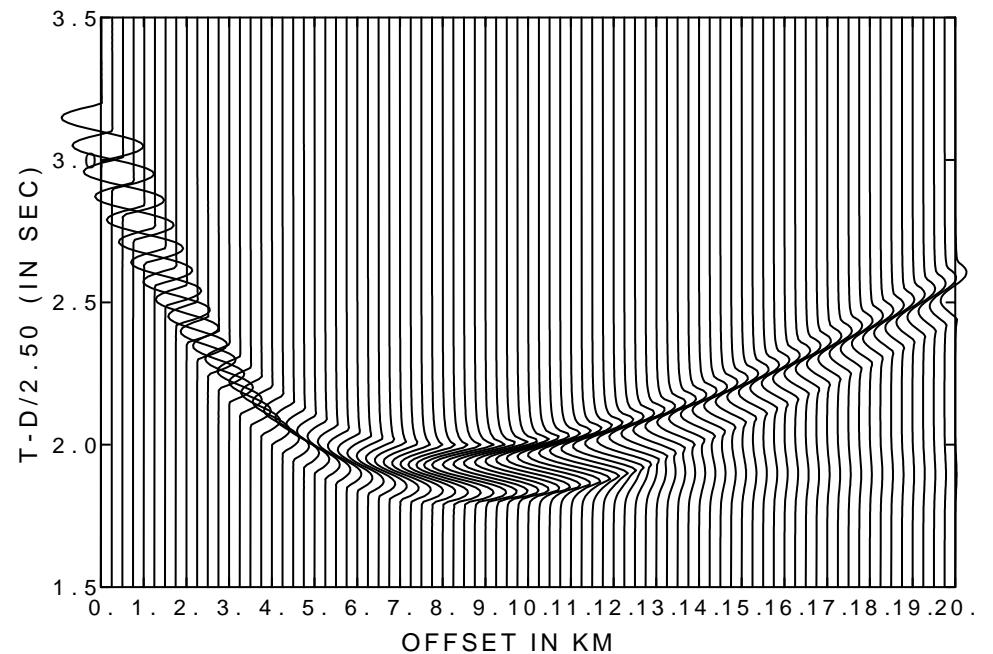
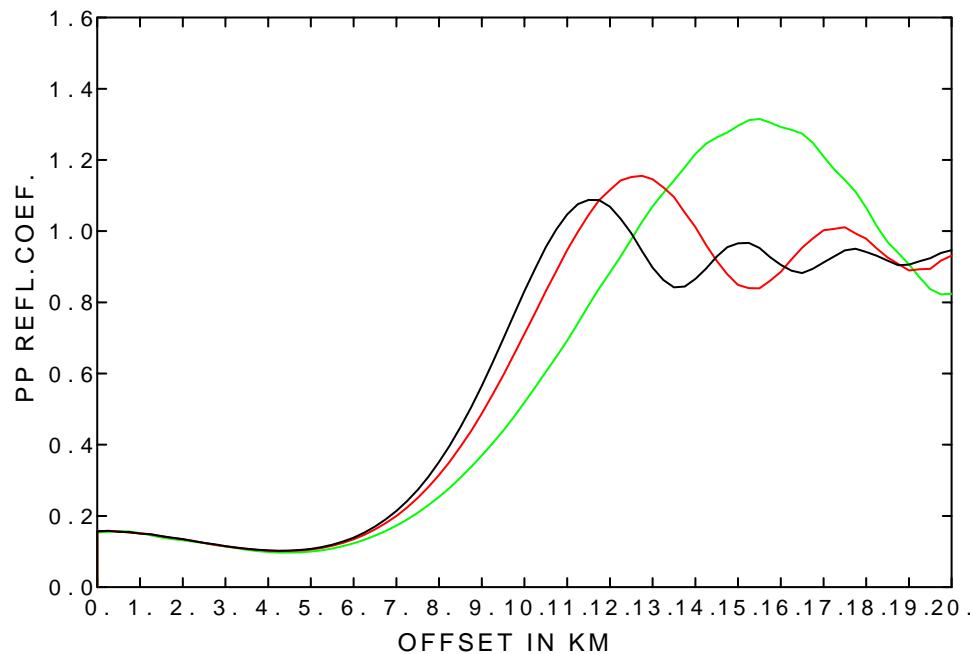
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$$f = 10 \text{ Hz}, \quad f = 20 \text{ Hz}, \quad f = 30 \text{ Hz}$$



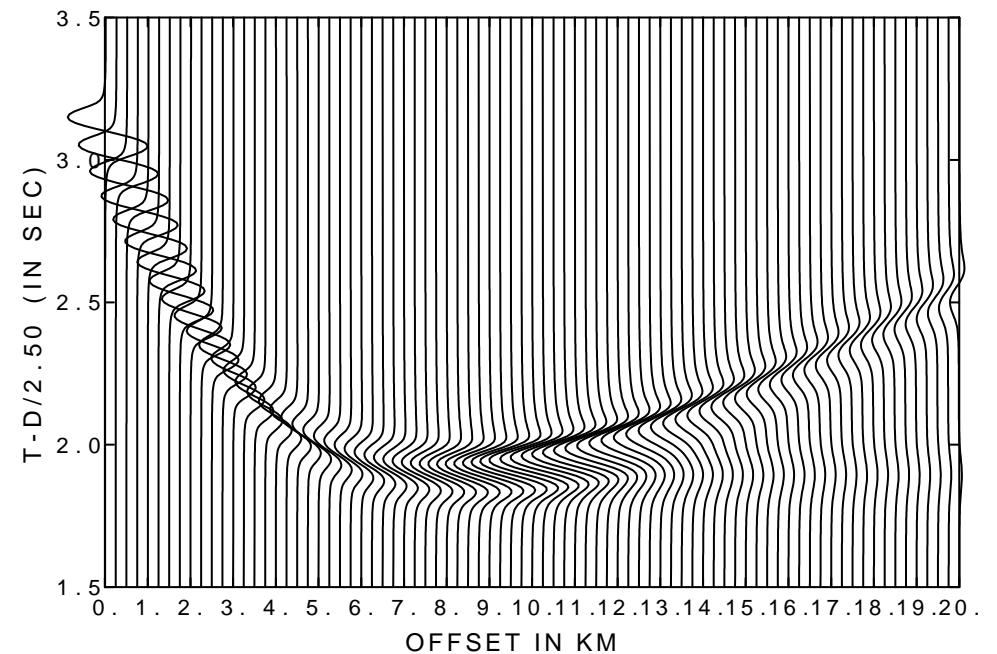
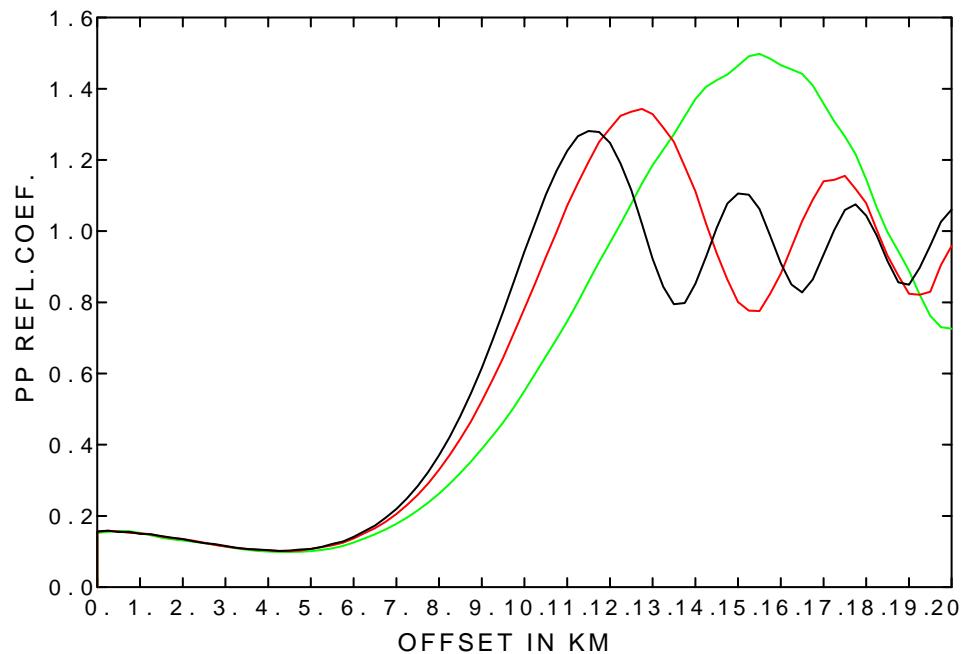
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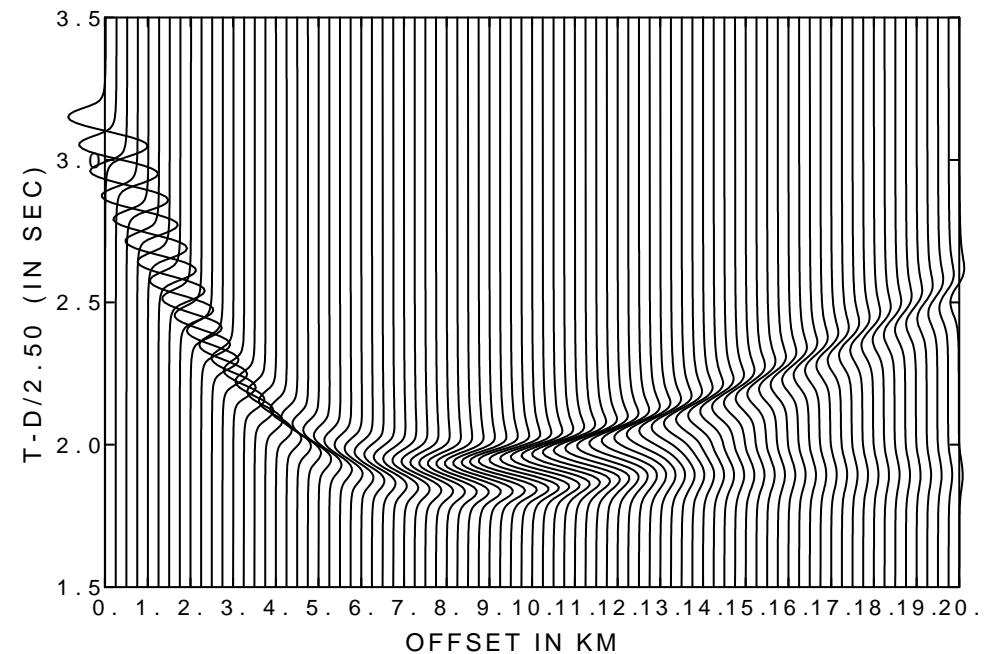
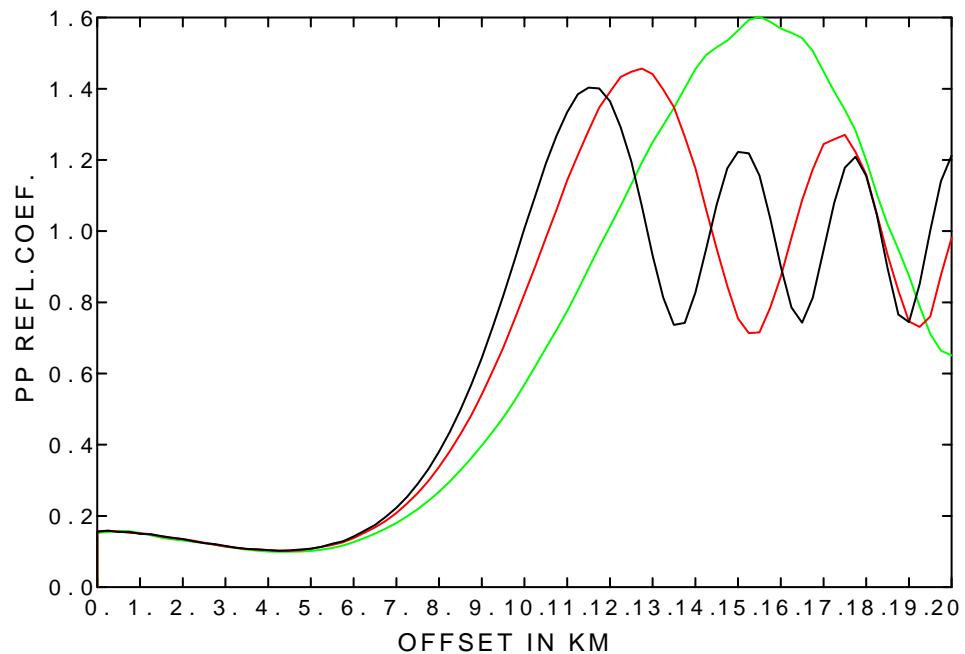
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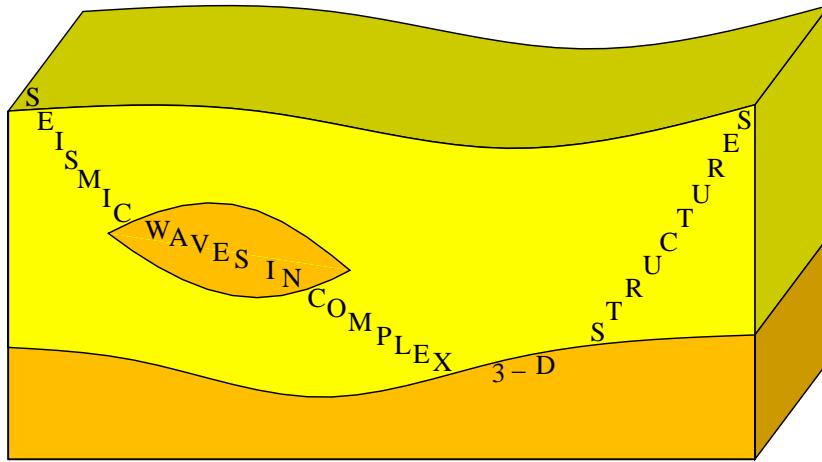
# Conclusions

- plane-wave PP coefficients in viscoelastic media difficult to use
- spherical-wave PP coefficients in viscoelastic media without problems
- spherical-wave seismograms Fourier transformed
  - ⇒ amplitudes and phases for chosen frequencies
- weak dependence of maximum amplitude position on  $Q$
- dependence of maximum of amplitude on  $Q$

# Possible future steps

- more extensive numerical tests
- use of viscoelastic anisotropic media
- determination of  $r^*$  from the position of the maximum  $r^M$   
and from the frequency (Červený, 1965)
- use of phases (Zhu & McMechan, 2012)

# Acknowledgements



Rongjiang Wang for his reflectivity code (Wang, 1999)

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